

Solving Systems by Using Elimination: Day 1 Notes

Name: Note Key

Objective: I can solve systems of equations by elimination.

Elimination Method:

- 1) Multiply equations by a number so that one variable has opposite coefficients.
- 2) Add the equations to eliminate one of the variables.
- 3) Solve the resulting equation for the variable.
- 4) Substitute that answer into either of the original equations to find the value for the other variable.
- 5) Write solution as an ordered pair (x,y).

Solve by substitution.

$$\begin{array}{r}
 \text{a) } x - y = 3 \\
 + x + y = 7 \\
 \hline
 2x = 10 \\
 \frac{2x}{2} = \frac{10}{2} \\
 x = 5
 \end{array}
 \quad \rightarrow \quad
 \begin{array}{r}
 5 + y = 7 \\
 -5 \quad -5 \\
 \hline
 y = 2
 \end{array}$$

$(5, 2)$

$$\begin{array}{r}
 \text{b) } 3x - 3y = 3 \\
 -x + 3y = -27 \\
 \hline
 2x = -24 \\
 \frac{2x}{2} = \frac{-24}{2} \\
 x = -12
 \end{array}
 \quad \xrightarrow{\text{#1)}} \quad
 \begin{array}{r}
 3(-12) - 3y = 3 \\
 -36 - 3y = 3 \\
 +36 \quad +36 \\
 \hline
 -3y = 39 \\
 \frac{-3y}{-3} = \frac{39}{-3} \\
 y = -13
 \end{array}$$

$(-12, -13)$

c) $5x + y = 15$

$$\begin{array}{r}
 (5x + y = 15) - 1 \\
 5x + y = 2 \\
 \hline
 -5x - y = -15 \\
 \hline
 0 = -13
 \end{array}$$

No solution
parallel lines

$$\begin{array}{r}
 d) 3x - 4y = -5 \\
 -3x + 4y = 5 \\
 \hline
 0 = 0
 \end{array}$$

infinitely many solutions
same line

Solve.

In a class, 46 students take the SAT exam. The number of boys is 8 more than the number of girls. Write a system that models the situation and solve.

$$\begin{array}{r}
 g + b = 46 \\
 -g + b = 8 \\
 \hline
 2b = 54 \\
 \frac{2b}{2} = \frac{54}{2} \\
 b = 27
 \end{array}
 \qquad
 \begin{array}{r}
 b = 8 + g \\
 -g \quad -g \\
 \hline
 b - g = 8 \\
 \\
 g + 27 = 46 \\
 -27 \quad -27 \\
 \hline
 g = 19
 \end{array}$$

boys: 27
girls: 19

What kind of coefficients of x and y are needed to solve a system by adding equations?

one needs to be the opposite of the other
you don't need both opposite

Solving Systems by Using Elimination: Day 2 Notes

Objective: I can solve systems of equations by elimination.

Name: Note Key

Elimination Method:

- 1) **Multiply** equations by a number so that one variable has opposite coefficients.
- 2) **Add** the equations to eliminate one of the variables.
- 3) **Solve** the resulting equation for the variable.
- 4) **Substitute** that answer into either of the **original** equations to find the value for the other variable.
- 5) Write solution as an **ordered pair** (x, y).

If you don't have equal coefficients for both variables, can you still use the elimination method?

Yes, you only need equal coefficients for one so you can multiply one by -1 to cancel it out

Solve by substitution.

a) $3x - 5y = -2$
 $(x + 3y = 4) \cdot -3$

$$\begin{array}{r} 3x - 5y = -2 \\ -3x - 9y = -12 \\ \hline -14y = -14 \\ \frac{-14y}{-14} = \frac{-14}{-14} \\ y = 1 \end{array}$$

$x + 3(1) = 4$
 $-3 \quad -3$
 $x = 1$

$(1, 1)$

b) $(x + 2y = 6) \cdot 2$
 $2x - 4y = -12$
 $2x + 4y = 12$

$$\begin{array}{r} 4x = 0 \\ \frac{4x}{4} = \frac{0}{4} \\ x = 0 \end{array}$$

$0 + 2y = 6$
 $\frac{2y}{2} = \frac{6}{2}$
 $y = 3$

$(0, 3)$

$$\begin{aligned} \text{c) } 3x - y &= -1 \\ y &= 3x - 5 \\ -3x \quad -3x \end{aligned}$$

$$y - 3x = -5$$

$$\begin{array}{r} 3x - y = -1 \\ -3x + y = -5 \\ \hline \end{array}$$

$$0 = -6$$

No solution

parallel lines

$$\begin{aligned} \text{d) } (-4x - 3y = 5) \cdot 3 &\rightarrow -12x - 9y = 15 \\ (3x - 2y = -8) \cdot 4 &\rightarrow 12x - 8y = -32 \end{aligned}$$

$$3x - 2(1) = -8$$

$$\begin{array}{r} 3x - 2 = -8 \\ +2 \quad +2 \end{array}$$

$$\frac{3x}{3} = \frac{-6}{3}$$

$$x = -2$$

$$\boxed{(-2, 1)}$$

$$\begin{array}{r} -17y = -17 \\ \hline -17 \quad -17 \end{array}$$

$$y = 1$$

$$\begin{aligned} \text{e) } 12x - 8y &= 18 \\ 6x &= 4y + 9 \\ -4y \quad -4y \end{aligned}$$

$$6x - 4y = 9$$

$$\begin{array}{r} 12x - 8y = 18 \\ (6x - 4y = 9) \cdot 2 \\ \hline \end{array}$$

$$12x - 8y = 18$$

$$-12x + 8y = -18$$

$$0 = 0$$

infinitely many solutions

same lines